potato leafhopper data

	Obs	time	treat	treat2	treat3
	1	2.3	control	control	control
	2	1.7	control	control	control
7	3	3.6	sucrose	sucrose	sugar
	4	4.0	sucrose	sucrose	sugar
	5	3.0	glucose	sixcarb	sugar
	6	2.8	glucose	sixcarb	sugar
	7	2.1	fructose	sixcarb	sugar
	8	2.3	fructose	sixcarb	sugar

time is the response variable (time until 50% of the insects in the cage died)

treat is the indicator (classification or grouping) variable for the full model with 4 means

treat2 is the indicator (classification or grouping) variable for the reduced model with 3 means

treat3 is the indicator (classification or grouping) variable for the most reduced model with 2 means



full model with 4 means (C,F,G,S)

The GLM Procedure

Coefficients for Estimate fructose vs glucose Row 1 Intercept 0 treat control 0 treat fructose 1 treat glucose -1 treat sucrose 0 Λ These are the coefficients of the linear combination used to compare the full model with the reduced model. The contrast here is between the fructose mean and the glucose mean. The full model has means: mu_C, mu_F, mu_G, mu_S The reduced model has means: mu_C, mu_(sixcarb), mu_S To move to the reduced model we need mu_F = mu_G, or equivalently, mu_F-mu_G = 0

			\sim												
						Sur	n of					K			
		Sour	rce		DF	Squa	ires	Mean So	quare	r Value	Pr > F				
	(Mode	el		3	3.97500	000	1.3250	00000	17.67	0.0090	F			
	7	Erro	r		4	0.30000	000	0.0750	00000				\searrow		
		Corr	ected 1	otal	7	4.27500	000								
/							_				The	overal	I F-test	<u></u>	
				R-Sc	uare	Coeff Var	Ro	ot MSE	time N	lean	H_C): the 4	means	are the same	
The basic ANO	/A			0.97	9825	10 04996	5 0	273861	2 72	5000					
table for the full	model			0.52	.5025	10.04550		.2/ 5001	2.72		R				
		[\neg	\checkmark			
			Sourc	e D		ype I SS	Mear	n Square	F Valı	ue Pr>	F		The o	verall time mea	۱n
			treat		3 3.9	97500000	1.3	32500000	17.	67 0.00	90				
		[Sourc	e D	ғ ту	/pe III SS	Mear	n Square	F Valu	ue Pr >	F				
			treat		3 3.9	97500000	1.3	32500000	17.	67 0.00	90				
		l													
	[Combr				Carta	+ 66	Maan		E Value					
		Contr	ast			- Contras	51 55	wean s	square	F value	Pr > F	_	>		
		fructo	se vs g	lucos	e 1	0.4900	00000	0.490	000000	6.53	0.0629				
'\															
	Daramat			E et	imata	Standa	ard	t Value		059/	Confidor				
$\langle \rangle$	Faramete			ES	inate				Fi > jų	95%			>	>	
	fructose	vs gluo	cose	-0.700	00000	0.273861	28	-2.56	0.0629	-1.460	36081 0	0.060360	81	-	
								-1		N					
The contrast sum of so	nuares ar	d E-te	est for			1				_'\					
comparing the full mod	del (C,F,G	G,S) ai	nd the	redu	ced		/				\				
model (C,sixcarb,S).									This	s hox co	ntains t	he esti	mate an	d	
H 0. mu F = mu G (w	ve do not	need	the fu	ll mo	del)				con	fidence	interval	for	mate an	4	
•					,				mu_	_F-mu_	G				
P-value = .0629									plus	s the t-te	est for				
We fail to reiect H 0 a	nd conclu	ude tha	at we	do no	ot .	X			H_C): mu_F	-mu_G	= 0			
need separate means	for the tw	o six	carbo	n sug	ar										
groups.					/										
The t-test is equalvale	nt to the I	-test		/											



reduced model with 3 means (C,sixcarb,S)

Class Level Information							
Class	Levels	Values					
treat2	3	control sixcarb sucrose					

Number of Observations Read	8
Number of Observations Used	8

reduced model with 3 means (C,sixcarb,S)

The GLM Procedure

Dependent Variable: time

	Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
(Model	2	3.48500000	1.74250000	11.03	0.0147
	Error	5	0.79000000	0.15800000	\mathcal{I}	
7	Corrected Total	7	4.27500000			

The basic ANOVA table for the reduced model with 3 means

R-Square	Coeff Var	Root MSE	time Mean
0.815205	14.58687	0.397492	2.725000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
treat2	2	3.48500000	1.74250000	11.03	0.0147

Source	DF	Type III SS	Mean Square	F Value	Pr > F
treat2	2	3.48500000	1.74250000	11.03	0.0147

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F	
6-carbons vs sucrose	1	2.08333333	2.08333333	13.19	0.0150	

	Parameter	Estimate	Standard Error	t Value	Pr > t	95% Confid	lence Limits	
\neg	6-carbons vs sucrose	-1.25000000	0.34423829	-3.63	0.0150	-2.13489269	-0.36510731	

The contrast sum of squares and F-test for comparing the reduced model (C,sixcarb,S) and the most reduced model (C,sugar).

H_0: mu_sixcarb = mu_S (we do not need the 3 means model)

P-value = .0150 (strong evidence mu_sixcarb notequl mu_S)

We reject H_0 and conclude that we DO NEED separate means for the sixcarb group and the sucrose group.

The t-test is equivalent to the t-test in the 6-carbons vs sucrose line

95% confidence interval for mu_sixcarb - mu_S

With 95% confidence, mu_S is between .3651 and 2.1349 days larger than mu_sixcarb



most reduced model with 2 means (C,sugar) Friday, June 22, 2018 09:25:27 AM 9

Class Level Information									
Class	Levels	Values							
treat3	2	control sugar							

Number of Observations Read	8
Number of Observations Used	8

most reduced model with 2 means (C,sugar)

The GLM Procedure

Dependent Variable: time

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	1.40166667	1.40166667	2.93	0.1380
Error	6	2.87333333	0.47888889	\square	
Corrected Total	7	4.27500000			
	Source Model Error Corrected Total	SourceDFModel1Error6Corrected Total7	Source DF Sum of Squares Model 1 1.40166667 Error 6 2.8733333 Corrected Total 7 4.2750000	Source DF Sum of Squares Mean Square Model 1 1.40166667 1.40166667 Error 6 2.87333333 0.47888889 Corrected Total 7 4.27500000 Image: Contemport of the state of the	Source DF Sum of Squares Mean Square F Value Model 1 1.40166667 1.40166667 2.93 Error 6 2.8733333 0.47888889 Corrected Total 7 4.2750000

The basic ANOVA table for the most reduced model with 2 means

R-Square	Coeff Var	Root MSE	time Mean
0.327875	25.39516	0.692018	2.725000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
treat3	1	1.40166667	1.40166667	2.93	0.1380

Source	DF	Type III SS	Mean Square	F Value	Pr > F
treat3	1	1.40166667	1.40166667	2.93	0.1380

	Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F	
K	control vs sugars	1	1.40166667	1.40166667	2.93	0.1380	

Parameter	Estimate	Standard Error	t Value	Pr > t	95% Confid	ence Limits	
control vs sugars	-0.96666667	0.56503032	-1.71	0.1380	-2.34924605	0.41591271	

This information is NOT NEEDED since we were not able to justify simplification of the model with 3 means to the model with 2 means



detailed analysis for the model with 3 means

		Class Le	evel Information	
	Class	Levels	Values	
`	treat2	3	control sixcarb sucrose] /
\mathbf{i}				
	Num	ber of Ob	servations Read 8	
	Num	ber of Ob	servations Used 8	

detailed analysis for the model with 3 means

The GLM Procedure

Dependent Variable: time

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	2	3.48500000	1.74250000	11.03	0.0147
Error	5	0.79000000	0.15800000		
Corrected Total	7	4.27500000			

R-Square	Coeff Var	Root MSE	time Mean
0.815205	14.58687	0.397492	2.725000

Source	DF	Type I SS	Mean Square	F Value	Pr > F
treat2	2	3.48500000	1.74250000	11.03	0.0147

Source	DF	Type III SS	Mean Square	F Value	Pr > F
treat2	2	3.48500000	1.74250000	11.03	0.0147

H 0 mu C = mu S						
	Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
H 0: mu sixcarb - mu S	control vs sucrose	1	3.24000000	3.24000000	20.51	0.0062
11_0. mu_sixcaib = mu_3	6-carbons vs sucrose	1	2.08333333	2.08333333	13.19	0.0150
H_0: mu_sixcarb=mu_C	6-carbons vs control	1	0.40333333	0.40333333	2.55	0.1710
	sucrose vs others	1	3.38272727	3.38272727	21.41	0.0057

 $H_0: mu_S = (mu_C+mu_F+mu_G)/3$

mu C - mu S	Parameter	Estimate	Standard Error	t Value	Pr > t	95% Confid	ence Limits
mu_sixcarb - mu_S	control vs sucrose	-1.80000000	0.39749214	-4.53	0.0062	-2.82178607	-0.77821393
	6-carbons vs sucrose	-1.25000000	0.34423829	-3.63	0.0150	-2.13489269	-0.36510731
	S-carbons vs control	0.55000000	0.34423829	1.60	0.1710	-0.33489269	1.43489269
mu_sixcarb - mu_C	sucrose vs others	1.52500000	0.32958307	4.63	0.0057	0.67777975	2.37222025

mu_S - (mu_C+mu_F+mu_G)/3

These are comparison-wise (one at a time) hypothesis tests and confidence intervals. We need to make an adjustment for multiple comparisons. See the following for the experiment-wise simultaneous 95% confidence intervals.

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detailed analysis for the model with 3 means

The GLM Procedure

Scheffe's Test for time

Note: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than Tukey's for all pairwise comparisons.

Alpha	0.05
Error Degrees of Freedom	5
Error Mean Square	0.158
Critical Value of F	5.78614

	Comparisons significant at the 0.05 level are indicate by ***.					
	treat2 Comparison	Difference Between Means	Simultaneous 95% Confidence Limits			
	sucrose - sixcarb	1.2500	0.0790	2.4210	***	
	sucrose - control	1.8000	0.4478	3.1522	***	
_	sixcarb - sucrose	-1.2500	-2.4210	-0.0790	***	
	sixcarb - control	0.5500	-0.6210	1.7210		
	control - sucrose	-1.8000	-3.1522	-0.4478	***	
	control - sixcarb	-0.5500	-1.7210	0.6210		

pairwise comparisons

mu_S - mu_sixcarb

mu_S - mu_C

mu_sixcarb - mu_S

etc

These are simultaneous 95% confidence intervals.

An adjustment has been made to take into account multiple comparisons.



simultaneous Scheffe type intervals

Obs	differ	estimate	stderr	lowerCL	upperCL
1	c_s	-1.800	0.39749	-3.15219	-0.44781
2	6_S	-1.250	0.34424	-2.42103	-0.07897
3	6_C	0.550	0.34424	-0.62103	1.72103
4	S_(Cand6	1.525	0.32958	0.40382	2.64618

These are the simultaneous confidence intervals computed earlier. Here they were constructed manually to demonstrate the procedure.

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