analysis for both house design types

The UNIVARIATE Procedure Variable: gas type = extra

| summary of gas consumption for the 14 | | Basic Statistical Measures | | | | | |
|--|--|----------------------------|----------|---------------------|----------|--|--|
| | | Location | | Variability | | | |
| insulation | | Mean | 13.87143 | Std Deviation | 2.36364 | | |
| | | Median | 13.70000 | Variance | 5.58681 | | |
| | | Mode | 13.70000 | Range | 10.50000 | | |
| | | | | Interquartile Range | 2.30000 | | |

| | Tests for Normality | | | | | | |
|---|---------------------|------|----------|-----------|---------|------------------|--|
| | Test | St | atistic | p Val | ue | | |
| < | Shapiro-Wilk | w | 0.93277 | Pr < W | 0.3335 | \triangleright | |
| | Kolmogorov-Smirnov | D | 0.16723 | Pr > D | >0.1500 | | |
| | Cramer-von Mises | W-Sq | 0.085422 | Pr > W-Sq | 0.1649 | | |
| | Anderson-Darling | A-Sq | 0.507886 | Pr > A-Sq | 0.1721 | | |

| Quantiles (D | Quantiles (Definition 5) | | | | |
|--------------|--------------------------|--|--|--|--|
| Level | Quantile | | | | |
| 100% Max | 18.8 | | | | |
| 99% | 18.8 | | | | |
| 95% | 18.8 | | | | |
| 90% | 16.0 | | | | |
| 75% Q3 | 15.3 | | | | |
| 50% Median | 13.7 | | | | |
| 25% Q1 | 13.0 | | | | |
| 10% | 11.7 | | | | |
| 5% | 8.3 | | | | |
| 1% | 8.3 | | | | |
| 0% Min | 8.3 | | | | |

Test for normality assumption for the houses with extra insulation sample

The null hypothesis is that the data (the 14 gas consumption values) form a random sample from a normal distribution. The large P-value .3335 shows supports for the normality assumption.

<-----

The distribution is reasonably symmetric

med-min=5.4 max-med=5.1 very slight skewness to the left

| | Extreme Values | | | | | | | | |
|--------|----------------|-------|------|---------|-------|------|--|--|--|
| Lowest | | | | Highest | | | | | |
| | Order | Value | Freq | Order | Value | Freq | | | |
| | 1 | 8.3 | 1 | 9 | 14.6 | 1 | | | |
| | 2 | 11.7 | 1 | 10 | 15.3 | 1 | | | |
| | 3 | 12.7 | 1 | 11 | 15.6 | 1 | | | |
| | 4 | 13.0 | 1 | 12 | 16.0 | 1 | | | |
| | 5 | 13.4 | 1 | 13 | 18.8 | 1 | | | |

The UNIVARIATE Procedure Variable: gas type = standard

summary of gas consumption for the 12 houses with standard insulation

| | Basic Statistical Measures | | | | | |
|----------|----------------------------|---------------------|----------|--|--|--|
| Location | | Variability | | | | |
| Mean | 16.76667 | Std Deviation | 2.99586 | | | |
| Median | 18.00000 | Variance | 8.97515 | | | |
| Mode | 13.90000 | Range | 10.30000 | | | |
| | | Interquartile Range | 5.00000 | | | |

Note: The mode displayed is the smallest of 3 modes with a count of 2.

| | Tests for Normality | | | | | | |
|---|---------------------|------|----------|-----------|--------|--|--|
| | Test | Sta | atistic | p Valı | | | |
| < | Shapiro-Wilk | w | 0.927281 | Pr < W | 0.3522 | | |
| | Kolmogorov-Smirnov | D | 0.243046 | Pr > D | 0.0483 | | |
| | Cramer-von Mises | W-Sq | 0.097949 | Pr > W-Sq | 0.1076 | | |
| | Anderson-Darling | A-Sq | 0.514106 | Pr > A-Sq | 0.1574 | | |

| Quantiles (Definition 5) | | | | |
|--------------------------|----------|--|--|--|
| Level | Quantile | | | |
| 100% Max | 21.70 | | | |
| 99% | 21.70 | | | |
| 95% | 21.70 | | | |
| 90% | 19.00 | | | |
| 75% Q3 | 18.95 | | | |
| 50% Median | 18.00 | | | |
| 25% Q1 | 13.95 | | | |
| 10% | 13.90 | | | |
| 5% | 11.40 | | | |
| 1% | 11.40 | | | |
| 0% Min | 11.40 | | | |

Test for normality assumption for the houses with standard insulation sample

The null hypothesis is that the data (the 12 gas consumption values) form a random sample from a normal distribution. The large P-value .3522 shows supports for the normality assumption.

The distribution is slightly skewed to the left but reasonably symmetric (The Shapiro-Wilk test supports this claim)

med-min=6.6 max-med=3.7 slight skewness to the left

| Extreme Values | | | | | | | | |
|----------------|-------|------|---------|-------|------|--|--|--|
| Lowest | | | Highest | | | | | |
| Order | Value | Freq | Order | Value | Freq | | | |
| 1 | 11.4 | 1 | 5 | 18.0 | 2 | | | |
| 2 | 13.9 | 2 | 6 | 18.1 | 1 | | | |
| 3 | 14.0 | 1 | 7 | 18.9 | 1 | | | |
| 4 | 15.3 | 1 | 8 | 19.0 | 2 | | | |
| 5 | 18.0 | 2 | 9 | 21.7 | 1 | | | |

energy usage summary (both house designs) Friday, June 15, 2018 02:51:26 PM 3

| - | | | Th | e TTES Varial | T Proce | dure | samp stanc | le means and lard deviation | t s | | |
|----------------------------|------------|---------------|-------|------------------|------------|---------|---------------|--------------------------------|-------------|-------------------|------|
| | type | Method | N | Mean | Std Dev | Std Err | Minim | um Maximum |] | | |
| | extra | | 14 | 13.8714 | 2.3636 | 0.6317 | 8.3 | 000 18.8000 | | | |
| | standard | | 12 | 16.7667 | 2.9959 | 0.8648 | 11.4 | 000 21.7000 | | | |
| | Diff (1-2) | Pooled | | -2.8952 | 2.6720 | 1.0512 | | | | | |
| | Diff (1-2) | Satterthwaite | | -2.8952 | | 1.0710 | | | | | |
| check for common popula | ation |]_/ | | | | | | pooled sar | nple stan | idard deviation | |
| variance: | | type | Meth | od | Mean | 95% C | L Mean | | | | |
| The ratio of the sample st | tandard | extra | | | 13.8714 | 12.5067 | 15.236 | 2 | | | |
| is between 1/2 and 2 | 070275 | standard | | | 16.7667 | 14.8632 | 18.670 | 1 | | | |
| so the assumption of a co | ommon (| Diff (1-2) | Pool | ed | -2.8952 | -5.0648 | -0.725 | 7 5 | % confide | ence interval for | 1 |
| population valiance ie en | · | Diff (1-2) | Satte | erthwaite | -2.8952 | -5.1234 | -0.667 | 0 <u>u</u> | (extra) - r | mu_(standard) | |
| | | | | | | | | _ | | | |
| | | Method | | Variance | s DF | t Value | Pr > t | | | | |
| | | Pooled | | Equal | 24 | -2.75 | 0.0110 | | | | |
| | | Satterthwa | ite | Unequal | 20.848 | -2.70 | 0.0134 | | | ו | |
| | | | | | | | | .0110 is the I | P-value fo | or | |
| | | | | Equality | of Varianc | es | | H_1: mu_(ex | tra) noteo | qual mu_(standa | ard) |
| | | Method | N | um DF | Den DF F | Value F | Pr > F | divide by 2 to | get the | P-value .0055 fc | or |
| | | Folded I | = | 11 | 13 | 1.61 0 | .4127 | H_1: mu_(ex | .tra) < mu | ı_(standard) | |

The TTEST Procedure Histograms with smoothed histograms

Variable: gas

Histograms with smoothed histograms (fitted density curves "kernel") and fitted normal density curves for each sample.



The TTEST Procedure

Variable: gas



The UNIVARIATE Procedure Variable: gas type = extra

summary of gas consumption for the 11 solar design houses with extra insulation

| | Basic Statistical Measures | | | | | | |
|--------|----------------------------|---------------------|---------|--|--|--|--|
| Loc | ation | Variability | | | | | |
| Mean | 14.22727 | Std Deviation | 2.72253 | | | | |
| Median | 14.50000 | Variance | 7.41218 | | | | |
| Mode | 15.70000 | Range | 8.50000 | | | | |
| | | Interquartile Range | 4.30000 | | | | |

| Tests for Normality | | | | | |
|---------------------|------|----------|-----------|---------|--|
| Test | St | atistic | p Value | | |
| Shapiro-Wilk | w | 0.956073 | Pr < W | 0.7219 | |
| Kolmogorov-Smirnov | D | 0.128473 | Pr > D | >0.1500 | |
| Cramer-von Mises | W-Sq | 0.033874 | Pr > W-Sq | >0.2500 | |
| Anderson-Darling | A-Sq | 0.227742 | Pr > A-Sq | >0.2500 | |

| Quantiles (I | Definition 5) |
|--------------|---------------|
| Level | Quantile |
| 100% Max | 19.0 |
| 99% | 19.0 |
| 95% | 19.0 |
| 90% | 17.6 |
| 75% Q3 | 15.7 |
| 50% Median | 14.5 |
| 25% Q1 | 11.4 |
| 10% | 11.3 |
| 5% | 10.5 |
| 1% | 10.5 |
| 0% Min | 10.5 |

Test for normality assumption for the houses with extra insulation sample

The null hypothesis is that the data (the 11 gas consumption values) form a random sample from a normal distribution. The large Pvalue .7219 shows supports for the normality assumption.

> The distribution is reasonably symmetric (The Shapiro-Wilk test

med-min=4 max-med=4.5

| Extreme Values | | | | | | | |
|----------------|-------|------|---------|-------|------|--|--|
| Lowest | | | Highest | | | | |
| Order | Value | Freq | Order | Value | Freq | | |
| 1 | 10.5 | 1 | 6 | 14.5 | 1 | | |
| 2 | 11.3 | 1 | 7 | 15.2 | 1 | | |
| 3 | 11.4 | 1 | 8 | 15.7 | 2 | | |
| 4 | 12.6 | 1 | 9 | 17.6 | 1 | | |
| 5 | 13.0 | 1 | 10 | 19.0 | 1 | | |

supports this claim)

The UNIVARIATE Procedure Variable: gas

type = standard

| Basic Statistical Measures | | | | | | | | |
|----------------------------|----------|---------------------|---------|--|--|--|--|--|
| Loc | ation | Variability | | | | | | |
| Mean | 16.13750 | Std Deviation | 2.07906 | | | | | |
| Median | 16.40000 | Variance | 4.32250 | | | | | |
| Mode | | Range | 7.60000 | | | | | |
| | | Interquartile Range | 3.35000 | | | | | |

| | Tests for Normality | | | | | |
|-----------|---------------------|-----------|----------|-----------|---------|------------------|
| | Test | Statistic | | p Value | | |
| \langle | Shapiro-Wilk | w | 0.959144 | Pr < W | 0.6463 | \triangleright |
| | Kolmogorov-Smirnov | D | 0.132841 | Pr > D | >0.1500 | |
| | Cramer-von Mises | W-Sq | 0.054795 | Pr > W-Sq | >0.2500 | \ |
| | Anderson-Darling | A-Sq | 0.337386 | Pr > A-Sq | >0.2500 | |

| Quantiles (I | Quantiles (Definition 5) | | | | |
|--------------|--------------------------|---|--|--|--|
| Level | Quantile | | | | |
| 100% Max | 19.90 | | | | |
| 99% | 19.90 | | | | |
| 95% | 19.90 | | | | |
| 90% | 18.00 | | | | |
| 75% Q3 | 17.70 | l | | | |
| 50% Median | 16.40 | | | | |
| 25% Q1 | 14.35 | | | | |
| 10% | 13.30 | | | | |
| 5% | 12.30 | | | | |
| 1% | 12.30 | | | | |
| 0% Min | 12.30 | | | | |

| Extreme Values | | | | | | |
|----------------|--------|-------|-------|--|--|--|
| Low | Lowest | | nest | | | |
| Order | Value | Order | Value | | | |
| 1 | 12.3 | 12 | 17.6 | | | |
| 2 | 13.3 | 13 | 17.8 | | | |
| 3 | 13.7 | 14 | 17.9 | | | |
| 4 | 13.8 | 15 | 18.0 | | | |
| 5 | 14.9 | 16 | 19.9 | | | |

Test for normality assumption for the houses with standard insulation sample The null hypothesis is that the data (the 16

gas consumption values) form a random sample from a normal distribution. The large P-value .6463 shows supports for the normality assumption.

> The distribution is slightly skewed to the left but reasonably symmetric (The Shapiro-Wilk test supports this claim)

med-min=4.1 max-med=3.5 slight skewness to the left

The TTEST Procedure

| | | | Variab | le: gas | K | s s | ample mea tandard de | ans and eviations |
|-----------------------------|---------------|----|---------|---------|---------|---------|-------------------------|----------------------|
| type | Method | N | Mean | Std Dev | Std Err | Minimum | Maximum | |
| extra | | 11 | 14.2273 | 2.7225 | 0.8209 | 10.5000 | 19.0000 | |
| standard | | 16 | 16.1375 | 2.0791 | 0.5198 | 12.3000 | 19.9000 | |
| Diff (1-2) | Pooled 1 | | -1.9102 | 2.3576 | 0,9234 | | | |
| Diff (1-2) | Satterthwaite | | -1.9102 | | 0.9716 | | | |
| pooled sample standard devi | | | | | | | | |

check for common population variance:

The ratio of the sample standard deviations 2.7225/2.0791 = 1.3095 is between 1/2 and 2 so the assumption of a common population variance is OK

| / | | | | | | |
|-------|-------|---------------|---------|---------|----------|-------------------------------|
| type | | Method | Mean | 95% C | L Mean | |
| extra | a | | 14.2273 | 12.3983 | 16.0563 | |
| stan | dard | | 16.1375 | 15.0296 | 17.2454 | |
| Diff | (1-2) | Pooled | -1.9102 | -3.8120 | -0.00841 | ← 95% confidence interval for |
| Diff | (1-2) | Satterthwaite | -1.9102 | -3.9537 | 0.1333 | mu_(extra) - mu_(standard) |
| | | | | | | - |

| Method | Variances | DF | t Value | Pr > t | | |
|---------------|-----------|--------|---------|---------|---|---|
| Pooled | Equal | 25 | -2.07 | 0.0491 | ~ | / |
| Satterthwaite | Unequal | 17.726 | -1.97 | 0.0652 | ' | |

| Equality of Variances | | | | | | |
|-----------------------|--------|--------|---------|--------|--|--|
| Method | Num DF | Den DF | F Value | Pr > F | | |
| Folded F | 10 | 15 | 1.71 | 0.3344 | | |

.0491 is the P-value for H_1: mu_(extra) notequal mu_(standard)

divide by 2 to get the P-value .02455 for H_1: mu_(extra) < mu_(standard)

Variable: gas

Histograms with smoothed histograms (fitted density curves "kernel") and fitted normal density curves for each sample.



The TTEST Procedure

Variable: gas

